

Cal. of K from  $\Delta G^\circ$

$\Delta G^\circ = -RT \ln K$ , given is a way to evaluate the value of K (eqn constt) from std-free energy  $\Delta G^\circ$  data

(1) From std. free energy calculations  $\Delta G^\circ$  of the reactants & products  $\Delta G^\circ = \sum \Delta G^\circ_f(P) - \sum \Delta G^\circ_f(R)$  where  $\Delta G^\circ_f$  for elements in their std state is taken as zero

(2) From  $\Delta H^\circ$  obtain calorimetrically or from Hess' law  $\Delta S^\circ$  from third law entropies  
 $\Delta G^\circ = \Delta H^\circ - T \Delta S^\circ$

(3) using statistical mechanics & certain information about  $\phi$ . molecule obtained from spectroscopic data

(4) From emf data using  $\Delta G^\circ = -nF E^\circ$

Variation of Equilibrium Constant with Temp

The eq<sup>n</sup> constt  $K_p$  & standard free energy of a general reaction  $aA + bB \rightleftharpoons mN + nO$  are related as

$\Delta G^\circ = -RT \ln K_p$  &  $\Delta G^\circ = (m \mu_N^\circ + n \mu_O^\circ) - (a \mu_A^\circ + b \mu_B^\circ)$   
 $-RT \ln K_p = (m \mu_N^\circ + n \mu_O^\circ) - (a \mu_A^\circ + b \mu_B^\circ)$

Diff w.r.t temp at constt

$$\frac{d \ln K_p}{dT} = -\frac{1}{R} \left[ \frac{m}{R} \left( \frac{\partial \mu_N^\circ}{\partial T} \right) + n \frac{\partial}{\partial T} \left( \frac{\mu_O^\circ}{R} \right) - \left( a \frac{\partial}{\partial T} \left( \frac{\mu_A^\circ}{R} \right) + b \frac{\partial}{\partial T} \left( \frac{\mu_B^\circ}{R} \right) \right) \right]$$

$$\left( a \frac{\partial}{\partial T} \left( \frac{\mu_A^\circ}{R} \right) + b \frac{\partial}{\partial T} \left( \frac{\mu_B^\circ}{R} \right) \right)$$

From Gibbs Helmholtz eq.  $\frac{\partial}{\partial T} \left( \frac{\Delta G^\circ}{T} \right) = -\frac{\Delta H^\circ}{T^2}$  (19)

$\frac{H_{im}^\circ}{T}$  is partial molar enthalpy of the substance in the standard state

$$\frac{d \ln K_p}{dT} = \frac{-1}{RT^2} \left[ (-m H_{im}^\circ - n H_{in}^\circ) - (-a H_{am}^\circ - b H_{bn}^\circ) \right]$$

$$= \frac{-1}{RT^2} \left[ \sum H^\circ(P) - \sum H^\circ(R) \right]$$

$$\frac{d \ln K_p}{dT} = \frac{-1}{RT^2} \Delta H^\circ \quad \text{--- (20)}$$

This eq. is called van't Hoff eq.  $\frac{d \ln K_p}{dT}$  relates the rate of change of eq<sup>n</sup> const. with temp to the heat of reaction. <sup>with the heat of reaction</sup>  $\frac{d \ln K_p}{dT}$  tells the rate of change of eq<sup>n</sup> const. with temp, whether K will ↑ or ↓ depends upon the nature of reaction whether it is exothermic, endothermic or athermic.

(1) (a) For exothermic reaction  $\Delta H^\circ$  is negative, R.H.S. of eq (20) is negative so with increase of temp,  $\frac{d \ln K_p}{dT}$  is  $\frac{-ve}{T^2}$  therefore to make R.H.S. +ve  $d \ln K_p$  and  $K_p$  should be -ve i.e. decrease

(b) When  $\Delta H^\circ$  is +ve, then  $\ln K_p$  and  $K_p$  should +ve ↑ that means increase in equilibrium const. means increase in conc<sup>n</sup> of products. That means in exothermic reactions, formation of products is favoured with lowering of temp.

That is why  $\text{NH}_3$  is synthesized at low temp



(21)

For endothermic reaction,  $\Delta H^\circ$  is positive, R.H.S.



If  $\Delta H^\circ$  is +ve, then  $K_p$  and  $K_c$  will  
 increase. That means increase in equilibrium constant  
 means increase in conc<sup>n</sup> of products. That  
 means in exothermic reaction, formation of  
 products is favoured with lowering of temp  
 that is why  $\text{NH}_3$  is synthesized at low temp  
 $\text{N}_2 + 3\text{H}_2 \rightleftharpoons 2\text{NH}_3 \quad \Delta H^\circ = -92.4 \text{ kJ}$

(23)

- (21) For endothermic reaction,  $\Delta H^\circ$  is positive,  $R \ln K$   
 of eq<sup>n</sup> is positive. So with increase of temp  
 $\Delta T$  is positive should be  $K_p$  should increase &  
 $K_c$  increase. In endothermic reaction, the  
 formation of product is favoured with increase of temp.
- (22) For athermic reaction,  $\Delta H^\circ$  is zero, the eq<sup>n</sup> constant  
 $K_p$  is independent of temperature.

Variation of  $K_c$  with Temp

$$RT \ln [K_c \left(\frac{C^\circ RT}{P^\circ}\right)^{\Delta\nu}] = -\Delta G^\circ$$

$$\ln K_c + \Delta\nu \ln T + \Delta\nu \ln \frac{C^\circ R}{P^\circ} = -\frac{\Delta G^\circ}{R}$$

on differentiating w.r.t. T

$$\frac{d \ln K_c}{dT} + \frac{\Delta\nu}{T} + 0 = -\frac{1}{R} \frac{\partial}{\partial T} \left[ \frac{\Delta H^\circ}{T} \right]$$

$$\frac{d \ln K_c}{dT} + \frac{\Delta\nu}{T} = \frac{\Delta H^\circ}{RT^2}$$

$$\frac{d \ln K_c}{dT} = \frac{\Delta H^\circ}{RT^2} - \frac{\Delta\nu}{T}$$

$$\frac{d \ln K_c}{dT} = \frac{\Delta H^\circ - \Delta\nu RT}{RT^2}$$

$\Delta H^\circ = \Delta E^\circ + \Delta\nu RT$  for an ideal gas

$$\Delta E^\circ = \Delta H^\circ - \Delta\nu RT \text{ or } \Delta H^\circ - \Delta\nu RT$$

$$\frac{d \ln K_c}{dT} = \frac{\Delta E^\circ}{RT^2} \text{ where } \Delta E^\circ \text{ is change of}$$

internal energy in a reaction and is heat change  
 when reaction occurs at const T & V

When  $\Delta n = 0$  like  $H_2 + I_2 \rightleftharpoons 2HI$ ,  $K_p = K_c$  (2)  
 $\Delta H^\circ = \Delta E^\circ$

When  $\Delta n \neq 0$ , then  $K_p$  &  $K_c$  have different Temp. Coefficient

Variation of Equilibrium const with Pressure

$K_p$  &  $K_c$  are independent of Pressure for ideal gases, but  $K_x$  is pressure dependant

(1)  $RT \ln K_p = -\Delta G^\circ$  where  $\Delta G^\circ$  is standard free energy of the reaction when the reactant & products of a chemical reaction are at standard state of 1 atm P and is the function of temperature only  
 $K_p$  is function of Temp. only & independent of Pressure

$$\left( \frac{\partial \ln K_p}{\partial P} \right)_T = - \frac{\partial}{\partial P} \left( \frac{\Delta G^\circ}{RT} \right)_T = 0$$

It means that the amounts of reactants & products at equilibrium do not change. There is change in the amount so that  $K_p$  is not changed.

$N_2O_4 \rightleftharpoons 2NO_2$  with  $\uparrow$  of P,  $\propto$   $N_2O_4$  degree of dissociation of  $N_2O_4$  decrease, while  $\downarrow$  of P  $\uparrow$   $\propto$   
 $\therefore K_p = \frac{4x^2 P}{1-x^2}$

Calc  $\rightarrow$  -

NPA



(2)  $K_c$  is independent of  $P$

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$$K_p = K_c \left( \frac{C^{\circ} RT}{P} \right)^{\Delta n}$$
$$\ln K_p = \ln K_c + \Delta n \ln \frac{C^{\circ} RT}{P}$$

Diff wrt  $P$  keeping  $T$  const

$$\left( \frac{\partial \ln K_p}{\partial P} \right)_T = \left( \frac{\partial \ln K_c}{\partial P} \right)_T + \frac{\Delta n}{P} \left[ \Delta n \ln \left( \frac{C^{\circ} RT}{P} \right) \right]$$

$$0 = \left( \frac{\partial \ln K_c}{\partial P} \right)_T + 0$$

$$\left( \frac{\partial \ln K_c}{\partial P} \right)_T = 0$$

(3)  $K_c$  is pressure dependent  $K_p = K_c (P/p_0)^{\Delta n}$

$$\ln K_p = \ln K_c + \Delta n \ln P/p_0$$

$\ln K_c = \ln K_p - \Delta n \ln (P/p_0)$  Diff wrt  $P$  at const  $T$

$$\left( \frac{\partial \ln K_c}{\partial P} \right)_T = \left( \frac{\partial \ln K_p}{\partial P} \right)_T - \frac{\Delta n}{P/p_0}$$

$$\left( \frac{\partial \ln K_c}{\partial P} \right)_T = \left( -\frac{\Delta n}{P/p_0} \right) - \Delta n \quad \Delta n = \sum \text{Mole of } P - \sum \text{Mole of } R$$

(1) when  $\Delta n = 0$ ,  $K_p = K_c = K_a$ ,  $K_p$  is independent of  $P$   
 $H_2 + I_2 \rightleftharpoons 2HI$  ;  $CO_2 + H_2 \rightleftharpoons H_2O + CO$

(2) when there is  $\downarrow$  in mole nos.  $\Delta n < 0$ ,  $K_p$   $\uparrow$  with  $\uparrow$  of  $P$ , i.e. more product is formed with  $\downarrow$  of  $P$ ,  $K_c$  will  $\downarrow$ , product will  $\downarrow$



The reaction is carried out at high pressure

(3) if  $\Delta n > 0$ , there is increase in no. of moles 23

$K_c$   $\downarrow$  with  $\uparrow$  in pressure as

when  $\Delta n = 0$ ,  $K_p = K_c = K_x$ ,  $K_p$  is independent of  $P$   
 $H_2 + I_2 \rightleftharpoons 2HI$ ,  $CO_2 + H_2 \rightleftharpoons H_2O + CO$

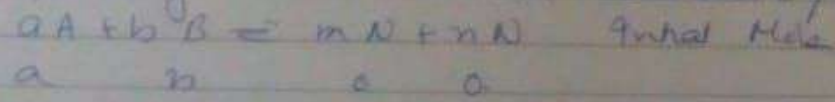
(2) when there is  $\downarrow$  in mole nos.  $\Delta n < 0$ ,  $K_p$  is  $\uparrow$  with  $\uparrow$  of  $P$ , i.e. more product is formed with  $\downarrow$  of  $P$ , i.e. it will  $\downarrow$ , product will  $\downarrow$   
 eg.  $N_2 + 3H_2 \rightleftharpoons 2NH_3$ ,  $\Delta n = -2$

The reaction is carried out at high pressure

(3) if  $\Delta n > 0$ , there is increase in no. of moles, 23

$N_2O_4 \rightleftharpoons 2NO_2$ ,  $K_p \downarrow$  with  $\uparrow$  in pressure as R.H.S. of eq. (2) is -ve, & L.H.S. should also be -ve, with  $\uparrow$  in pressure, also  $K_p$  must be -ve i.e. less than zero

Effect of Inert Gas on Reaction Equilibrium



$a(1-x) \quad b(1-x) \quad mx \quad nx$  At equilibrium

Let  $x$  be the extent of reaction. The mole no. of different species at equilibrium

$n_A = a(1-x) = n_B = b(1-x)$ ,  $n_M = mx$ ,  $n_N = nx$

Total no. of moles =  $n_t = n_A + n_B + n_M + n_N$   
 $= a(1-x) + b(1-x) + mx + nx$   
 $= (a+b) + x(m+n-a-b)$   
 $= (a+b) + \Delta n x$

$x_A = \frac{a(1-x)}{(a+b) + \Delta n x}$        $x_B = \frac{b(1-x)}{(a+b) + \Delta n x}$        $x_M = \frac{mx}{(a+b) + \Delta n x}$

$x_N = \frac{nx}{(a+b) + \Delta n x}$

Partial Pressures are given by Dalton law  $P_i = x_i P$

$P_A = \frac{a(1-x)}{(a+b) + \Delta n x} P$ ,  $P_B = \frac{b(1-x)}{(a+b) + \Delta n x} P$ ,  $P_M = \frac{mx}{(a+b) + \Delta n x} P$

$P_N = \frac{nx}{(a+b) + \Delta n x} P$

Eq<sup>n</sup> const<sup>n</sup>  $K_p = \frac{(P_M)^m (P_N)^n}{(P_A)^a (P_B)^b}$