

UNIT-2

Modern physics

Atomic structure
Atom is stable # Atom shows line spectra # Atom is electrically neutral

model of Atom

Thomson model (Plum Pudding model)



Can be explained thermionic emission, photoelectric effect
But line spectra, intensity of variation of diff. line can't explained.

Rutherford model (1911)

- # Based on observations of α -scattering experiment on Au.
- # Nucleus contains all the charge & almost all of the mass of atom. Have radius 10^{-15} m.
- # electron revolves around nucleus in various shells.

Draw back:

Stability Problem:

e^- oscillates \rightarrow radiates \rightarrow spiral path

fall in nucleus
 \rightarrow unstable atom

Spectra:

Rutherford correlated the freq. ~~with~~ of spectral lines with angular freq. of e^- . But spiral freq. which has all freq. which shows atomic spectra continuous.

\Rightarrow Removal of these shortcomings results Bohr model.

Bohr model (1913)

- # (modified Rutherford model)
- # mixture of classical & non-classical ideas.

Two postulates:

1) Stationary orbit concept: only those orbits are possible for which

$$mvr = \frac{nh}{2\pi}$$

2) In Rutherford model, no quantification of energy level.

no oscillation in these orbits

3) Origin of spectra: Spectra arises due to transition between various energy level and not due to e^- revolution.

Discussion of H-atom & spectra (Here)

- # Can't explain intensity variation of spectral line
- # Unable to explain fine structure
- # valid only for simple system, not a complex system.
- # Couldn't explain the effect of Zeeman field on spectral line \Rightarrow Bohr Sommerfeld model

(8)

Bohr model

(Suggested by Bohr in 1913)

Three Postulates:

- (i) e^- revolves in the circular path under Coulombian attraction between nucleus & nucleus.
- (ii) Electron will revolve around a circular path for which the magnitude of angular momentum is integral multiple of $\frac{h}{2\pi}$.

These orbits are called stationary orbits.

$$i.e. \quad |\vec{L}| = m v e r_n = \frac{nh}{2\pi} = n\hbar$$

where $n=1, 2, 3, \dots$

When an e^- makes a transition from one orbit of total energy E_i to another orbit of total energy E_f , then emission or absorption of radiation takes place in the form of emitted or absorbed photon.

The energy emitted or absorbed is

$$h\nu = E_i - E_f \quad \text{For emission (i.e. } E_i > E_f) \quad \nu = \frac{E_i - E_f}{h}$$

and the frequency of radiation $\nu = \frac{E_i - E_f}{h}$

Explanation of spectrum of hydrogen like atom:

Let $+Ze \rightarrow$ charge of nucleus

$-e \rightarrow e^-$ charge

$m_e \rightarrow$ electron mass

The centripetal force is provided by Coulombian attraction.

$$\frac{m v^2}{r_n} = \frac{1}{4\pi\epsilon_0} \frac{(Ze)^2}{r_n^2}$$

$$\Rightarrow \frac{m^2 v^2 r_n^2}{r_n} = \frac{1}{4\pi\epsilon_0} \frac{Z^2 e^2}{r_n^2} m r_n^2$$

$$\Rightarrow \left(\frac{m v}{2\pi\hbar}\right)^2 \times \frac{1}{r_n} = \frac{Z^2 e^2}{4\pi\epsilon_0 r_n^2} \quad \text{as } m v r_n = \frac{nh}{2\pi}$$

(multiplying by $m v r_n^2$ on both sides)

or $m v r_n = \frac{nh}{2\pi}$

$$\Rightarrow r_n = \frac{nh^2}{m v_e^2}; n=1, 2, 3$$

$$\Rightarrow [n a_0 n^2]$$

For H-atom, $n=1, 2, 3$

$$\Rightarrow r_1 = \frac{h^2}{m v_e^2} = 6.6 \times 10^{-34} \times 8.85 \times 10^{-12} = 5.27 \times 10^{-11} \text{ m}$$

$$\Rightarrow [n = 0.53 \text{ \AA}] \text{ Called Bohr radius } r_0 \text{ or } a_0$$

$$\text{for } n=2, [r_2 = 4 r_1] \Rightarrow r_2 = 4 \times 0.53 \text{ \AA} = 2.12 \text{ \AA}$$

$$\# \text{ Now as } v_n = \frac{nh}{2\pi m r_n} = \frac{nh}{2\pi m n a_0}$$

$$\Rightarrow v_n = \frac{nh}{2\pi m n a_0} = \frac{nh}{2\pi m a_0} \left(\frac{nh^2}{m v_e^2} \right)^{-1/2}$$

$$\Rightarrow v_n = \frac{ze^2}{2nhc_0}, \text{ where } n=1, 2, 3$$

$$\# \text{ And the total energy } E_n = K.E + P.E = \frac{1}{2} m \left[\frac{ze^2}{2nhc_0} \right]^2 + \frac{-ze^2}{4\pi\epsilon_0 \left(\frac{nh^2}{m v_e^2} \right)}$$

after substituting by the in numerator & denominator

$$\Rightarrow E_n = -R_\infty \frac{z^2 hc}{n^2}, \text{ where } R_\infty = \frac{m e^4}{8 \epsilon_0^2 h^3 c}$$

$$R_\infty = \frac{m e^4}{8 \epsilon_0^2 h^3 c} = 1.097 \times 10^7 \text{ /m}$$

This is called Rydberg constant

$$\text{For Hydrogen } E_n = -\frac{R_\infty hc}{n^2}$$

$$\Rightarrow E_n = -\frac{13.6}{n^2} \text{ eV}$$

For $n=1$ $E_1 = 13.6 \text{ eV}$

$n=2$ $E_2 = 3.4 \text{ eV}$

$n=3$ $E_3 = 1.51 \text{ eV}$

$n \rightarrow \infty$ $E_\infty = 0 \text{ eV}$

NEA 

| | |
|-------|--------------------|
| $n=4$ | -0.85 eV |
| $n=3$ | -1.51 eV |
| $n=2$ | -3.4 eV |
| $n=1$ | -13.6 eV |

Minimum energy required to remove the e^- completely from the orbit is called binding energy or ionization energy.

Binding energy of Hydrogen = 13.6 eV
 Ionization energy of H = 13.6 eV
 Similarly ionization energy of $Li = 5.39 \text{ eV}$

Sometimes energy is expressed in terms of Fermi value (F)

$$T = \frac{E}{hc} = \bar{\nu} = \text{wave no. with unit m}^{-1} \text{ or cm}^{-1}$$

Thus, the wave no. of n th state = $-\frac{13.6z^2}{n^2} \text{ m}^{-1}$.

and $\boxed{\bar{\nu} = c\bar{\sigma}}$

where $\bar{\nu}$ = wave no.

c = vel. of light

$\bar{\sigma}$ = freq. of light.

Hydrogen atom

The observed data for hydrogen atom:

Simplest atom having one proton & one e⁻.

Shows a group of spectral lines called Lyman, Balmer, Paschen, Brackett & Pfund series.

① Lyman series (UV) region: $n_2 = 2, 3, 4, \dots$

$$\begin{aligned} \frac{1}{\lambda} &= \bar{\nu} = \frac{\sigma}{c} = \frac{1}{c} \left(\frac{E_1 - E_2}{h} \right) = \frac{1}{hc} (E_1 - E_2) \\ &= \frac{1}{hc} \left\{ \frac{-13.6z^2}{n_1^2} - \left(\frac{-13.6z^2}{n_2^2} \right) \right\} \\ &= \frac{1}{hc} \left\{ \frac{13.6z^2}{n_1^2} - \frac{13.6z^2}{n_2^2} \right\} \\ &= \frac{13.6z^2}{hc} \left\{ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right\} \end{aligned}$$

for Lyman series ~~$n_1 = 1$~~ , ~~$n_2 = 2, 3, 4, \dots$~~ all the transition will stop at $n=1$.

Also, Lyman series is observed when transition starts from $n=1$ or ends at $n=1$.

Absorption Spectra
Emission Spectra

$n=1$ starts
 $n=1$ ends

For emission $n=1 = hf$

and $n=2, 3, 4, \dots, n_i$

$$\frac{1}{\lambda} = \frac{13.6 z^2}{hc} \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right)$$

$$\frac{1}{\lambda} = R_{\infty} z^2 \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right)$$

Where R_{∞} is the Rydberg constant when nucleus is infinitely heavy in comparison to e^- .

$$R_{\infty} = \frac{m e^4}{8 \epsilon_0^2 h^3 c^3} = 1.097 \times 10^7 \text{ m}^{-1}$$

or $1.097 \times 10^5 \text{ cm}^{-1}$.

Series limit of Lyman: $n_f=1, n_i=\infty$.

~~This line of Lyman series will have highest frequency.~~

Ex: 1 Find the wavelength corresponding to α line in Lyman series.

α line in Lyman series is when

$$n_f=1, n_i=2$$

$$\frac{1}{\lambda_{\alpha}} = R_{\infty} (1)^2 \left(\frac{1}{1^2} - \frac{1}{2^2} \right) = R_{\infty} \left(1 - \frac{1}{4} \right) = \frac{3}{4} R_{\infty}$$

$$= 1.097 \times 10^7 \times \frac{3}{4} \text{ m}^{-1}$$

$$\frac{1}{\lambda_{\alpha}} = 0.82275 \times 10^7 \text{ m}^{-1} = \lambda_{\alpha}^{-1}$$

$$\Rightarrow \lambda_{\alpha} = \frac{1}{0.82275 \times 10^7}$$

$$= \frac{10^{-7}}{0.82275} = 1.215426 \times 10^{-7} \text{ m}$$

$$= 1215.4 \times 10^{-10} \text{ m}$$

$$\lambda_{\alpha} = 1215 \text{ \AA}$$

For β , $n_i=3, n_f=1, \Rightarrow \lambda_{\beta} = 1025 \text{ \AA}$

and series limit is when $n_i=\infty, n_f=1, \lambda_{\infty} =$

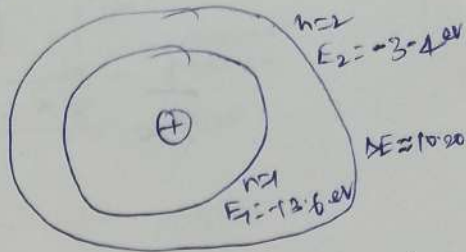
Ex: 2 Find the energy difference for α -line which have $\lambda_{\alpha} = 1215 \text{ \AA}$

Soln:

$$\lambda (\text{A}^{\circ}) = \frac{12400}{(\Delta E) \text{ eV}}$$

given, $\lambda_{\alpha} = 1215 \text{ \AA}$

$$\Rightarrow \Delta E (\text{eV}) = \frac{12400}{\lambda_{\alpha}} = \frac{12400}{1215} = 10.205 \text{ eV}$$



$$\Delta E = 10.205 \text{ eV} = E_2 - E_1 = 10.20 \text{ eV}$$

$$\frac{1}{1} - \frac{1}{9} = \frac{9-1}{36} = \frac{8}{36}$$

② Balmer series: $n_f = 2, n_i = 3, 4, 5, \dots \infty$

for α -line in Balmer series, $n_f = 2, n_i = 3$

$$\Rightarrow \frac{1}{\lambda_{\alpha}} = 1.097 \times 10^7 \text{ m}^{-1} \left(\frac{1}{2^2} - \frac{1}{3^2} \right)$$

$$= 1.097 \times 10^7 \times \frac{5}{36} = 0.1523 \times 10^7 \text{ m}^{-1}$$

$$\Rightarrow \lambda_{\alpha} = 6.5659 \times 10^7 \text{ m}$$

$$= 6565 \times 10^{-10} \text{ m}$$

$$\lambda_{\alpha} \approx 6565 \text{ \AA} \quad \text{Visible region}$$

$$(\Delta E)_{\alpha \text{ line}} = \frac{12400}{\lambda_{\alpha} (\text{A}^{\circ})} = \frac{12400}{6565} = 1.888 \text{ eV}$$

$$\Rightarrow (\Delta E)_{\alpha \text{ line}} = 1.888 \text{ eV}$$

Similarly λ_{β} for $n_f = 2, n_i = 4, \lambda_{\beta} = 486 \text{ \AA}, \lambda_{\gamma} = 4340 \text{ \AA}$
 λ_{δ} for $n_f = 2, n_i = \infty, \lambda_{\delta} = 3644 \text{ \AA}$

④ Paschen series: $\frac{1}{\lambda} = \bar{\nu} = R_{\infty} \left(\frac{1}{3^2} - \frac{1}{n^2} \right) \Rightarrow \lambda_{\infty} = 18746 \text{ \AA}$
 $n_f = 3, n_i = 4, 5, 6, \dots$

$$(\Delta E)_{\alpha} = \frac{12400}{18746} = 0.6614 \text{ eV}$$

$$\frac{1}{\lambda_{\infty}} = \bar{\nu} = R_{\infty} \left(\frac{1}{3^2} - \frac{1}{\infty} \right) = 8201 \text{ \AA}^{-1}$$

$$(\Delta E)_{\infty} = \frac{12400}{8201 \text{ \AA}} = 1.51 \text{ eV}$$

④ Brackett series: $n_f = 4, n_i = 5, 6, 7, 8, \dots \infty$
 $\downarrow \downarrow \downarrow \downarrow$
 $\alpha \quad \beta \quad \gamma \quad \delta$

$$\frac{1}{\lambda_{\alpha}} = R_{\infty} \left(\frac{1}{4^2} - \frac{1}{5^2} \right) \Rightarrow \lambda_{\alpha} = 40501 \text{ \AA}, \quad \Delta E_{\alpha} = \frac{12400}{40501} = 0.3061 \text{ eV}$$

$$\frac{1}{\lambda_{\infty}} = R_{\infty} \left(\frac{1}{4^2} - \frac{1}{\infty} \right) \Rightarrow \lambda_{\infty} = 14580, \quad \Delta E_{\infty} = 0.8504 \text{ eV}$$

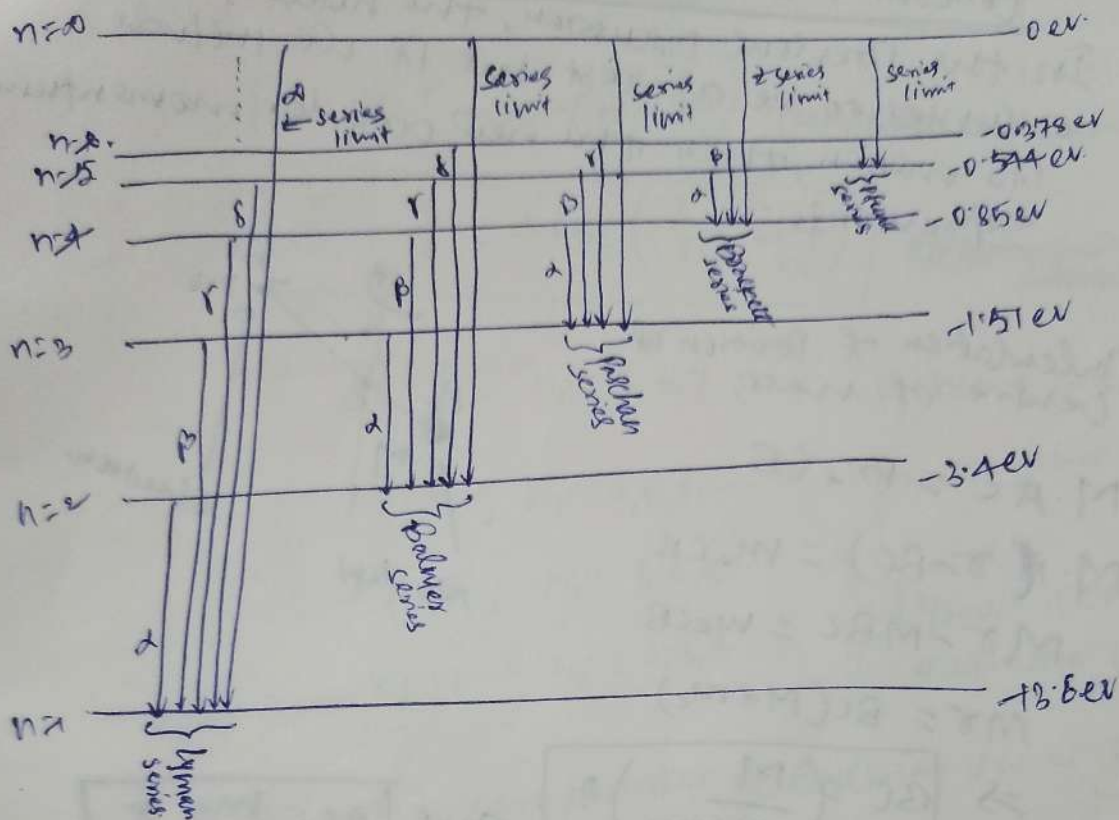
⑤ Pfund series: $n_f = 5, n_i = 6, 7, 8, 9, 10, \dots \infty$

$$\frac{1}{\lambda} = \bar{\nu} = R_{\infty} \left(\frac{1}{5^2} - \frac{1}{n_i^2} \right)$$

$$\lambda_{\alpha} = 74558 \text{ \AA}, \quad (\Delta E)_{\alpha} = 0.16631 \text{ eV}$$

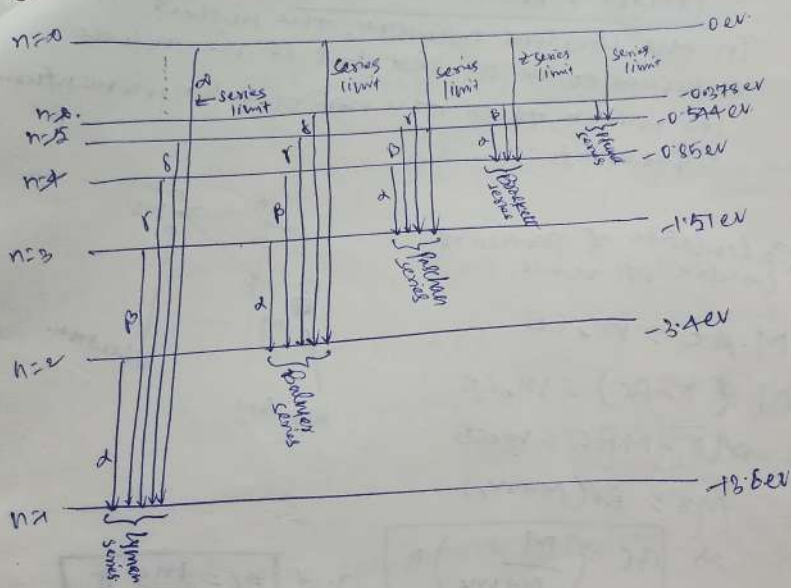
$$\lambda_{\infty} = 22782, \quad (\Delta E)_{\infty} = 0.5442 \text{ eV}$$

| Series | Wave no. | Region | α -line wavelength | Series limit (\AA) |
|------------|--|---------|---------------------------|-------------------------------|
| ① Lyman | $\bar{\nu} = \frac{1}{\lambda} = R \left(\frac{1}{1^2} - \frac{1}{n_i^2} \right)$ $n_i = 2, 3, 4, \dots$ | UV | 1215 \AA | 911 \AA |
| ② Balmer | $\bar{\nu} = \frac{1}{\lambda} = R \left(\frac{1}{2^2} - \frac{1}{n_i^2} \right)$ $n_i = 3, 4, 5, \dots$ | Visible | 6563 \AA | 3644 \AA |
| ③ Paschen | $\bar{\nu} = \frac{1}{\lambda} = R \left(\frac{1}{3^2} - \frac{1}{n_i^2} \right)$ $n_i = 4, 5, 6, \dots$ | IR | 18746 \AA | 8201 \AA |
| ④ Brackett | $\bar{\nu} = \frac{1}{\lambda} = R \left(\frac{1}{4^2} - \frac{1}{n_i^2} \right)$ $n_i = 5, 6, 7, \dots$ | IR | 40501 \AA | 14580 |
| ⑤ Pfund | $\bar{\nu} = \frac{1}{\lambda} = R \left(\frac{1}{5^2} - \frac{1}{n_i^2} \right)$ $n_i = 6, 7, 8, \dots$ | far IR | 74558 \AA | 22782 |



Shortcomings:

- ① Unable to explain intensity variation of spectral lines.
- ② Unable to explain the fine structure of.
- ③ Valid only for simple system, not for complex system.
- ④ Cannot explain the effect of electric & magnetic field on spectral lines.



Short Comings:

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