

Example

$$P_1 = 24 - Q_1$$

$$P_2 = 12 - 0.5Q_2$$

$$C = AC = MC = 6$$

$$D) P_1^*, P_2^*, Q_1^*, Q_2^*$$

for 1

$$TR = P_1 \times Q_1$$

$$R = Q_1 (24 - Q_1)$$

$$R = 24Q_1 - Q_1^2$$

$$\underline{MR = 24 - 2Q_1}$$

$$24 - 2Q_1 = 6$$

$$24 - 6 = 2Q_1$$

$$18 = 2Q_1$$

$$\underline{Q_1^* = 9}$$

$$\underline{P_1^* = 15}$$

$$\text{Profit} = TR_1 - TC$$

$$= \cancel{P_1^* \times Q_1}$$

$$(P_1^* - C) \times Q_1$$

$$= (15 - 6) \times 9$$

$$= 81$$

for 2

$$TR = P_2 Q_2$$

$$TR = (12 - 0.5Q_2) Q_2$$

$$TR = 12Q_2 - 0.5Q_2^2$$

$$\underline{MR = 12 - Q_2}$$

$$12 - Q_2 = 6$$

$$\underline{Q_2^* = 6}$$

$$\underline{P_2^* = 9}$$

$$\text{Profit} = TR_2 - TC$$

$$= (P_2^* - C) \times Q_2$$

$$= (9 - 6) \times 6$$

$$= 18$$

$$\text{Profit} = \pi_1 + \pi_2$$

$$= 81 + 18$$

$$\underline{\text{Profit} = 99}$$

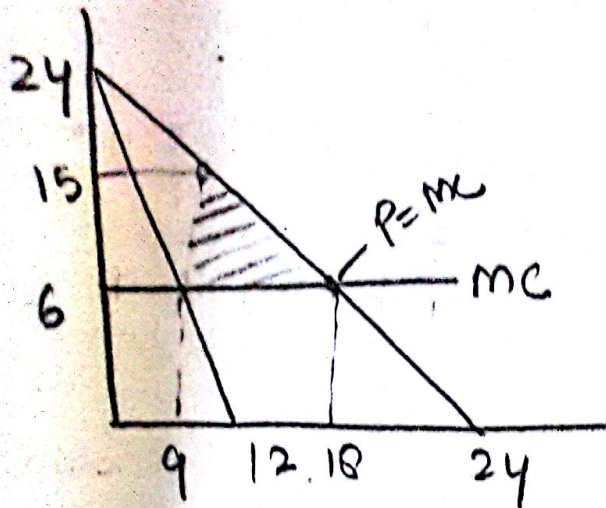
— Total monopoly profit.

$$3) DWL_1 = ?$$

$$DWL_2 = ?$$

$$0.5 Q_2 = 12$$

$$Q_2 = 24$$



$$\frac{1}{2} (18-9) (15-6)$$

$$\frac{1}{2} \times 9 \times 9$$

$$= \frac{81}{2} = 40.5$$

DWL

$$6 = 12 - 0.5 Q_2$$

$$6 = 0.5 Q_2$$

$$Q_2 = 12$$

$$\frac{1}{2} \times (12-6) (9-6)$$

$$= \frac{1}{2} \times 6 \times 3$$

$$= 9$$

$$DWL = DWL_1 + DWL_2$$

$$= 40.5 + 9$$

$$DWL = 49.5$$

Single price policy
if monopolist had to charge a uniform price then in this case he would stop serving market 2 and maximise profits by charging $P=15$ (uniform price) [only in this example not in general].
find out DWL in market 1 and market 2

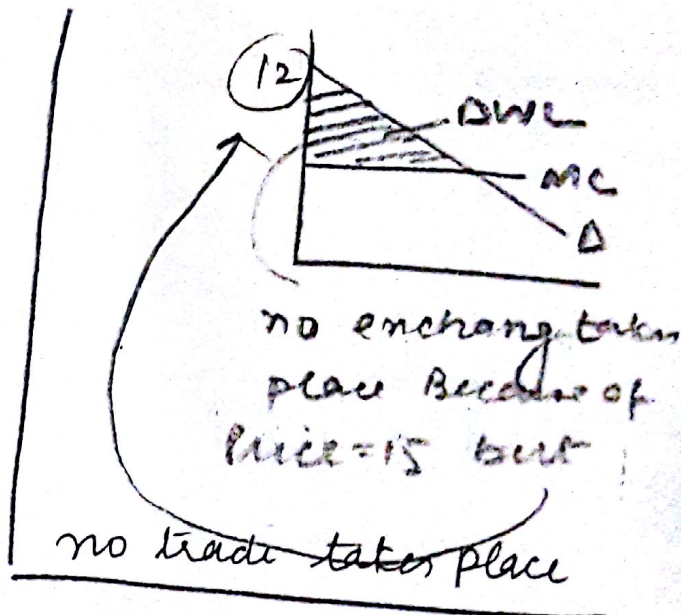
$$DWL_2 = \frac{1}{2} (12-6) (12-0)$$

$$= \frac{1}{2} \times 6 \times 12$$

$$DWL_2 = 36$$

$$\underline{DWL = DWL_1 + DWL_2 = 40.5 + 36}$$

$$\underline{DWL = 76.5}$$



DWL under uniform price policy exceeds then two price policy (111st Degree PD) hence we conclude that discrimination is some times welfare improving then single price policy.

IInd degree price discrimination

In linear two part tariff Consumers must pay a fixed fee for right to consume and (entry fee) uniform price for each unit consume (usage fee)

Example

amusement parks

Tariff is defined as

$$T(q) = \underbrace{a}_{\text{entry fee}} + \underbrace{pq}_{\text{usage fee}}$$

a = fixed fee / entry fee

P_2 marginal price

monopolist goal is to choose a and p so as to maximise profit.

Average price paid by consumer equal to

$$\bar{p} = \frac{I}{q}$$

$$\boxed{\bar{p} = \frac{a}{q} + p}$$

note)

Tariff is feasible only when those who pay low average price can not resell the good to those who ^{must} pay high average price

Case 1

monopolist can set $P = MC$ and $a =$ Consumer surplus of least eager buyer

Case 2

monopolist can set $P > MC$. ~~and~~ But here q decreases and some part of consumer surplus is converted into monopoly profit.

example

monopolist face two demand curves

$$q_1 = 24 - p_1 \Rightarrow p_1 = 24 - q_1 \quad MC = 6$$

$$q_2 = 24 - 2p_2 \Rightarrow p_2 = \frac{24}{2} - \frac{q_2}{2}$$

Ques) P is set $= MC$
find $a = ?$ and $p = ?$

$$0 = 12 - \frac{q_2}{2}$$

$$\pi = ?$$

find optimal part-tariff that maximize profit of monopoly such that $\pi = 2a + (P - MC)(q_1 + q_2)$