

Interference

Waves and optics

Q.1. A Plane light wave falls on Fresnel with an angle $\alpha = 2.0'$ between them. Determine the wavelength of light if the width of fringe on screen $\Delta x = 0.55 \text{ mm}$.

Solution

$$\Delta x = \frac{(a+b)\lambda}{2\alpha b} \quad \Delta x = 0.55 \text{ mm}$$

$$\alpha = 2.0'$$

$$\lambda = 2\alpha \Delta x = 0.64 \mu\text{m}$$

Q.2. The distance from Fresnel biprism to narrow slit and a screen are equal to $a = 25 \text{ cm}$ and $b = 100 \text{ cm}$ respectively. The refracting angle of glass biprism is equal to $\theta = 2.0'$. Find the wavelength of light if the width of the fringe on the screen is $\Delta x = 0.55 \text{ mm}$.

Solution :-
$$\Delta x = \frac{l\lambda}{d}$$

$$l = a + b$$

$$d = 2(n-1)\theta a$$

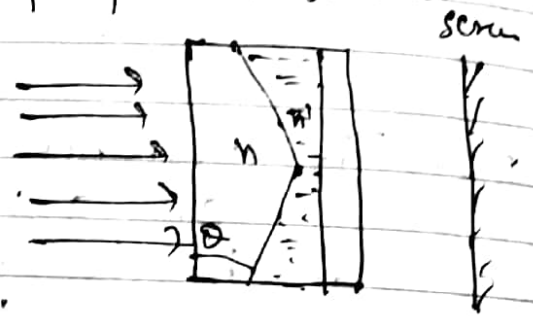
$$s = (n-1)\theta$$

$$d = 2s a$$

$n =$ refractive index of glass.

$$\text{then } \lambda = \frac{2(n-1)\theta a \Delta x}{a+b} = 0.64 \mu\text{m}$$

Q.3. A plane light wave with wavelength $\lambda = 0.70 \mu\text{m}$ falls normally on the base of biprism made of glass $n = 1.520$ with refracting angle $\theta = 5.0^\circ$ behind the prism there is plane-parallel plate, with the distance between filled with other liquid of refractive index $n' = 1.50$. Find the space between ~~them~~. Find the width of fringe on screen



Solution

It will be assumed the space between biprism and glass plate with other liquid constitute the complementary prism then the deviation

$$S = (n-1)\theta - (n'-1)\theta$$

$$= (n-n')\theta$$

$$d = 2a \cdot S$$

$$\Delta x = \frac{(a+b)\lambda}{2a\theta(n-n')}$$

$$\Delta x = \frac{\lambda}{2\theta(n-n')} = \frac{0.70}{2 \times 5 \times (1.520 - 1.50)}$$

$$= 0.2 \text{ mm}$$

Q.4. A plane monochromatic light wave falls normally on a diaphragm with two narrow slits separated by distance $d = 2.5 \text{ mm}$. A fringe pattern is formed on screen placed at a distance $l = 100 \text{ cm}$ behind the diaphragm. So what distance and in which direction will these fringes be displaced when one of the slits is covered by glass plate of thickness $h = 10 \mu\text{m}$.

Ans.

Extra phase difference produced by glass plate is

$$= \frac{2\pi}{\lambda} (n-1) h$$

this will cause shift equal to

$$\frac{(n-1) h}{\lambda} \text{ fringe width.}$$

by
$$\frac{(n-1) h}{\lambda} \times \frac{l \lambda}{d} = \frac{(n-1) h l}{d} = 2 \text{ m.}$$