

## Relation b/w $C_p$ and $C_v$

Specific heat at constant volume

$C_v$  → It is defined as the amount of heat required to raise the temp of one mole of gas through  $1^\circ\text{C}$  when volume kept const.

$$C_v = \left( \frac{dQ}{dT} \right)_v$$

Specific heat at const pressure

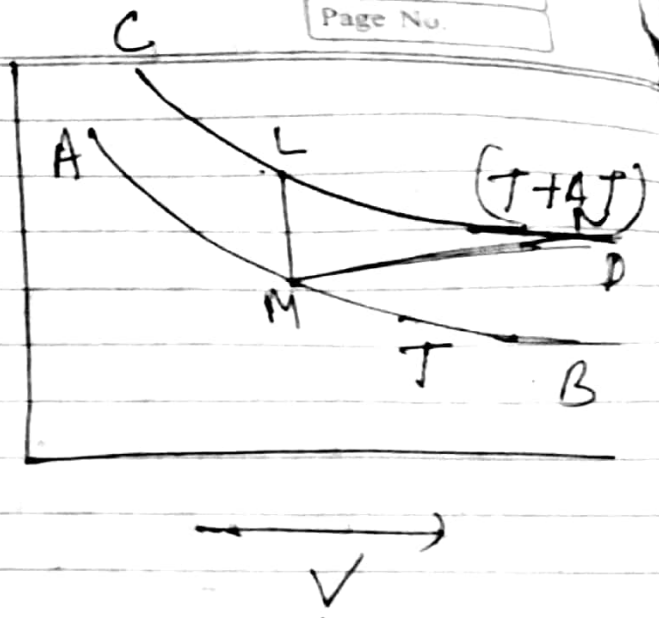
$C_p$  → It is defined as the amount of heat required to raise the temp of 1 mole of gas through  $1^\circ\text{C}$  when the pressure is kept const.

$$C_p = \left( \frac{dQ}{dT} \right)_p$$

Derivation of Mayer's formula.

$$\boxed{C_p - C_v = R}$$

The two  
isothermal  
AB and CD  
lines have Temp  
T and T + dT



M → L const volume.

$$dQ = dU + dW$$

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$$dW = P dV = 0$$

$$dQ = dU = U_L - U_M$$

$n = 1 \text{ mole}, S = C_V \Delta T$

$$dQ = 1 \times C_V \times dT$$

$$dQ = C_V dT$$

Change in internal energy  
in process

$$M \rightarrow N$$

$$U_N - U_M = \Delta Q - \Delta W$$

$$\Delta W = P \Delta V$$

$$U_N - U_M = C_p \Delta T - P \Delta V$$

Since gas is supposed to ideal  
gas so perfect gas equation

follows.  $P V = R T$

initial Point M, Pressure P

Temp T and at Point N ~~Pressure~~

Volume becomes  $V + \Delta V$

Temp  $T + \Delta T$

~~Heat Engine and~~

$$PV = RT \quad \text{--- (a)}$$

$$P(V + \Delta V) = R(T + \Delta T) \quad \text{--- (b)}$$

Subtracting (b) - (a)

$$P \Delta V = R \Delta T$$

Substituting  $P \Delta V = R \Delta T$

$$\underline{U_N - U_M} = C_p \Delta T - R \Delta T$$

So internal energy is only depend upon temp

$$U_N - U_M = U_N - U_M$$

$$C_v \Delta T = C_p \Delta T - R \Delta T$$

$$\boxed{C_p - C_v = R}$$