

B.Sc (H) Physics

27/10/2023

V Sem

Advanced Mathematical

Physics - I

(32227502)

Class Test (IA)

SET - ODD

M.M. 20

Time: 1 Hr

Q1 Attempt any 2 questions ($5 \times 2 = 10m$)

(a) Evaluate C^{20} , where $C = \begin{bmatrix} -1 & 3 \\ 1 & 1 \end{bmatrix}$

(b) Solve using matrix method

$$\dot{y} = z$$

$$\dot{z} = y$$

where $y(0) = 4, z(0) = 2$

(c) For a given matrix $A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}$,

prove that

$$\lambda^2 - \lambda \text{Tr}(A) + \det(A) = 0$$

(d) Find the condition for following matrix to be orthogonal

$$\begin{bmatrix} a+b & b-a \\ a-b & a+b \end{bmatrix}$$

Q2 Attempt any 2

(5 × 2 = 10 m)

(a) Show that transformation is linear
 $T(x, y, z) = (x - 4y, 3x + 2y - z, y + 2z)$

(b) If A, B, C are linearly independent vectors
determine if $A - B, B - C, C - A$ are
linearly dependent or not

(c) Show that the polynomial space of $\deg \leq n$
~~is a vector~~ and real coefficients forms a
vector space over the field $\mathbb{R}$.

(d) Consider the set^s of matrices
 $A(\alpha) = \begin{bmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{bmatrix}$, α is a real no.

Determine whether this set forms a group or
not under matrix multiplication (Assume that
matrix multiplication is associative).

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Advanced Mathematical
Physics - IClass Test (IA)SET - EVENTime: 1 HrMM: 20

Q1 Attempt any 2 questions (5×2=10m)

(a) If $B = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$, show that

$$e^{\theta B} = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$

(b) Verify Cayley-Hamilton theorem for the matrix $H = \begin{bmatrix} 3 & -1 \\ 4 & -2 \end{bmatrix}$ Hence find H^{-1}

(c) If P is non-singular matrix and $P^{-1}AP$ and $P^{-1}BP$ are diagonal matrices, then show that $AB=BA$

(d) Find the Eigen values and Eigen vectors of $A = \begin{bmatrix} 1 & 0 & 1 \\ 0 & 3 & 2 \\ 0 & 0 & 2 \end{bmatrix}$

Q2 Attempt - any 2 ($5 \times 2 = 10$ m)

(a) If W consists of all square matrices of order 2 with zero determinant, then determine whether W is a subspace of V or not.

(b) Linear transformation T on $\mathbb{R}^2$ is defined as
 $T(x, y) = (3x - 4y, x + 5y)$

Find the matrix representation of T relative to the Basis $f_1 = (1, 3)$, $f_2 = (2, 5)$

(c) Determine whether $(1, 2, 5)$, $(2, 5, 1)$, $(1, 5, 2)$ are linearly dependent or not

(d) Find the Basis & dimension of the W , a subspace of $\mathbb{R}^4$
 $W = \{ (a, b, c, d) : a + b = 0, c = 2d \}$

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